The Large-Misalignment Mechanism for the Formation of Compact Axion Structures

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arXiv:1909.11665

TRIUMF, Mar 12, 2020

Large Misalignment for Compact Axion Structures

Axions behave exactly like Cold Dark Matter (CDM)*

*except under certain conditions, on some length scales, and at times when they do not

Symmetry breaking after inflation: isocurvature fluctuations → axion strings & miniclusters

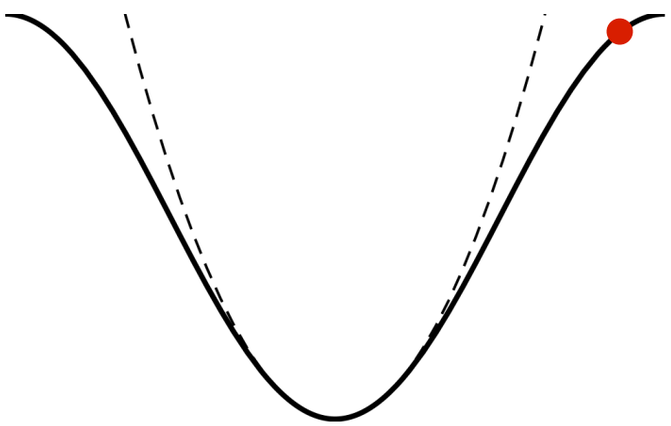
Symmetry breaking before inflation, small misalignment: density fluctuations suppressed below Jeans scale

Symmetry breaking before inflation, large misalignment:

density fluctuations enhanced for semi-relativistic modes when the axion starts oscillating

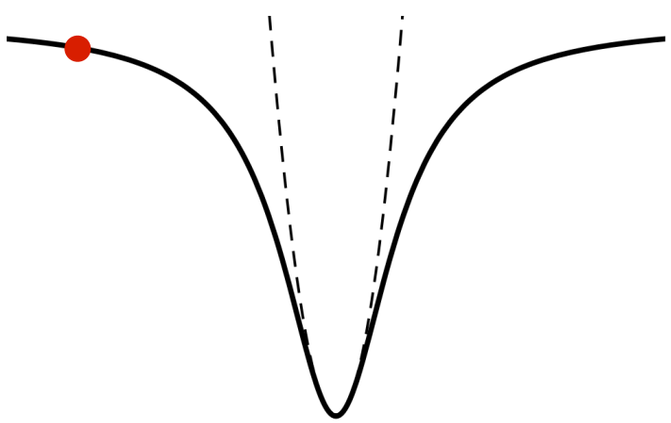
cosine

$$V = -m^2 f^2 \cos\frac{\phi}{f}$$



modulus

$$V = \frac{m^2 f^2}{2}\frac{\phi^2}{f^2+\phi^2}$$



QCD axion

$$V = -m_\pi^2 f_\pi^2 \sqrt{1 - \frac{4 m_u m_d}{(m_u+m_d)^2}\sin^2\left(\frac{a}{2f_a}\right)}$$

$$m_a(T) \approx \frac{m_u m_d}{m_u+m_d}\frac{m_\pi f_\pi}{f_a}$$

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$$\text{if } |\Theta_0| > \frac{\pi}{2}: \quad \text{for } \frac{k}{a} \sim m \sim H_{\rm osc}$$

$$\mathcal{B} \equiv \frac{\rho_s}{\rho_s^{\rm CDM}} \sim \exp\left\{\frac{m}{H_{\rm osc}}\right\} \qquad M_s^* \sim \frac{\rho_{\rm DM}^0}{(k_*)^3} \sim 5\times 10^9\,{\rm M}_\odot \left[\frac{10^{-22}\,{\rm eV}}{m}\right]^{3/2}$$

Large Misalignment Mechanism

$$\frac{\phi}{f} = \Theta(t) + \sum_{\mathbf{k}} \theta_{\mathbf{k}}(t) e^{i\mathbf{k}\cdot\mathbf{x}} \qquad \tilde{k}^2 \equiv \frac{k^2/a^2}{2mH}$$

3 ways to understand enhancement of structure formation:

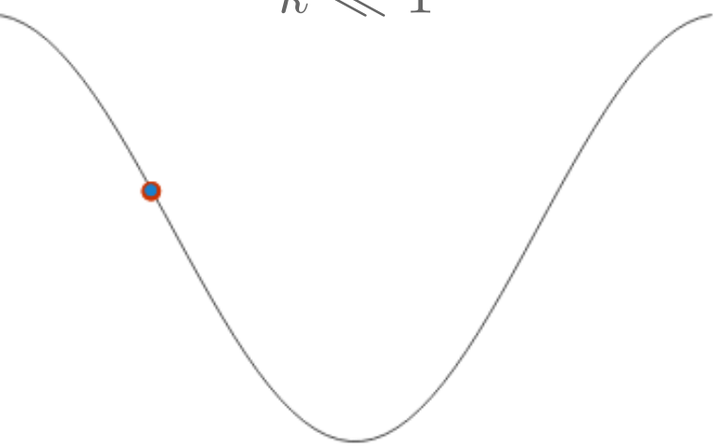
1. negative quartic → attractive self-interaction $\quad V = m^2 f^2 \left[1 - \cos\theta\right] \simeq m^2 f^2 \left[\frac{\theta^2}{2} - \frac{\theta^4}{24} + \ldots\right]$

2. density fluctuations have negative sound speed $\quad c_s^2 \simeq \frac{\mathbf{k}^2/a^2}{4m^2} - \frac{\rho}{8m^2 f^2}$

$$\delta_{\mathbf{k}} = 2\frac{\dot{\Theta}\dot{\theta}_{\mathbf{k}} + m^2\Theta\theta_{\mathbf{k}}}{\dot{\Theta}^2 + m^2\Theta^2} \qquad \ddot{\delta}_{\mathbf{k}} + 2H\dot{\delta}_{\mathbf{k}} - \left[4\pi G\rho - \frac{c_s^2\mathbf{k}^2}{a^2}\right]\delta_{\mathbf{k}} = 0$$

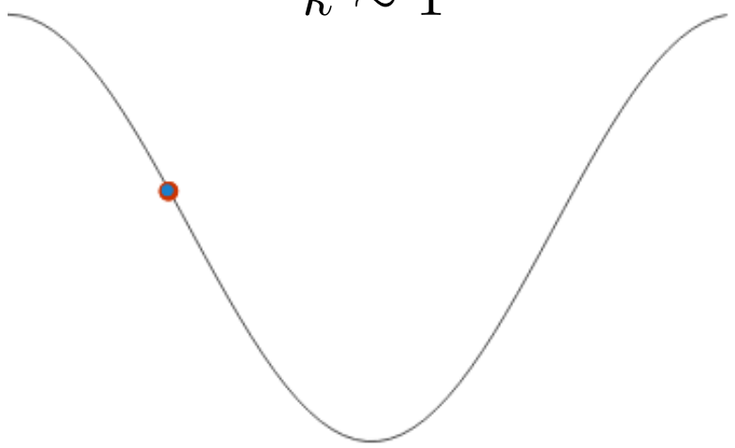
3. parametric resonance for field fluctuations

nonrelativistic mode $\tilde{k} \ll 1$



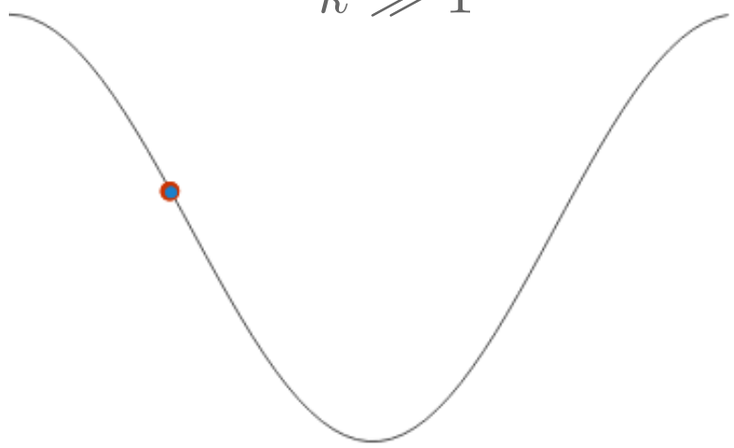
enters horizon when nonlinearities are small

semi-relativistic mode $\tilde{k} \sim 1$



frequency match; nonlinearity > friction

ultra-relativistic mode $\tilde{k} \gg 1$



frequency mismatch; curvature fluctuation damped

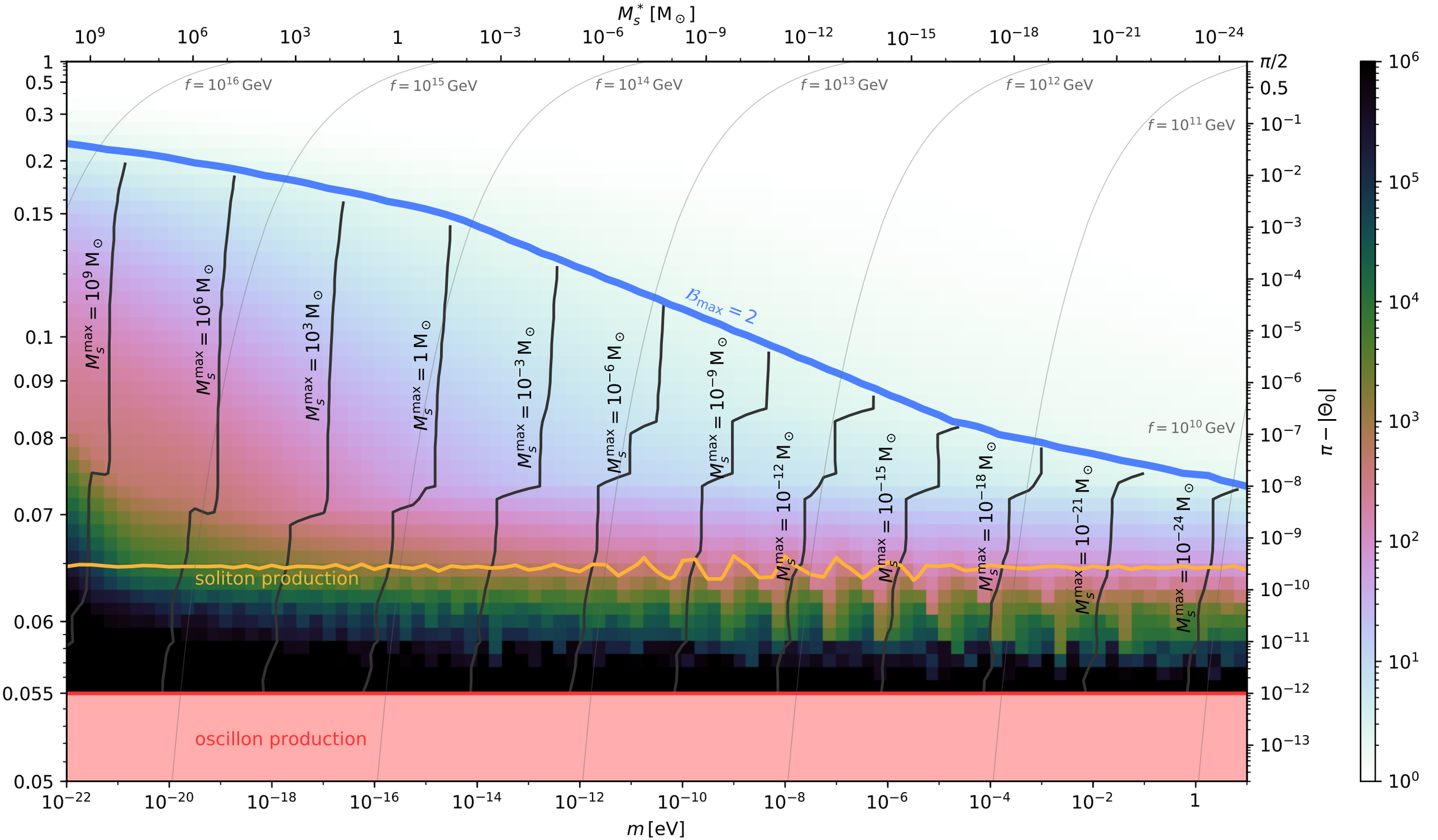
Compact Axion Structures

$$f_{\pi/2} \sim M_{\rm Pl} \left(\frac{H_{\rm eq}}{m} \right)^{1/4}$$

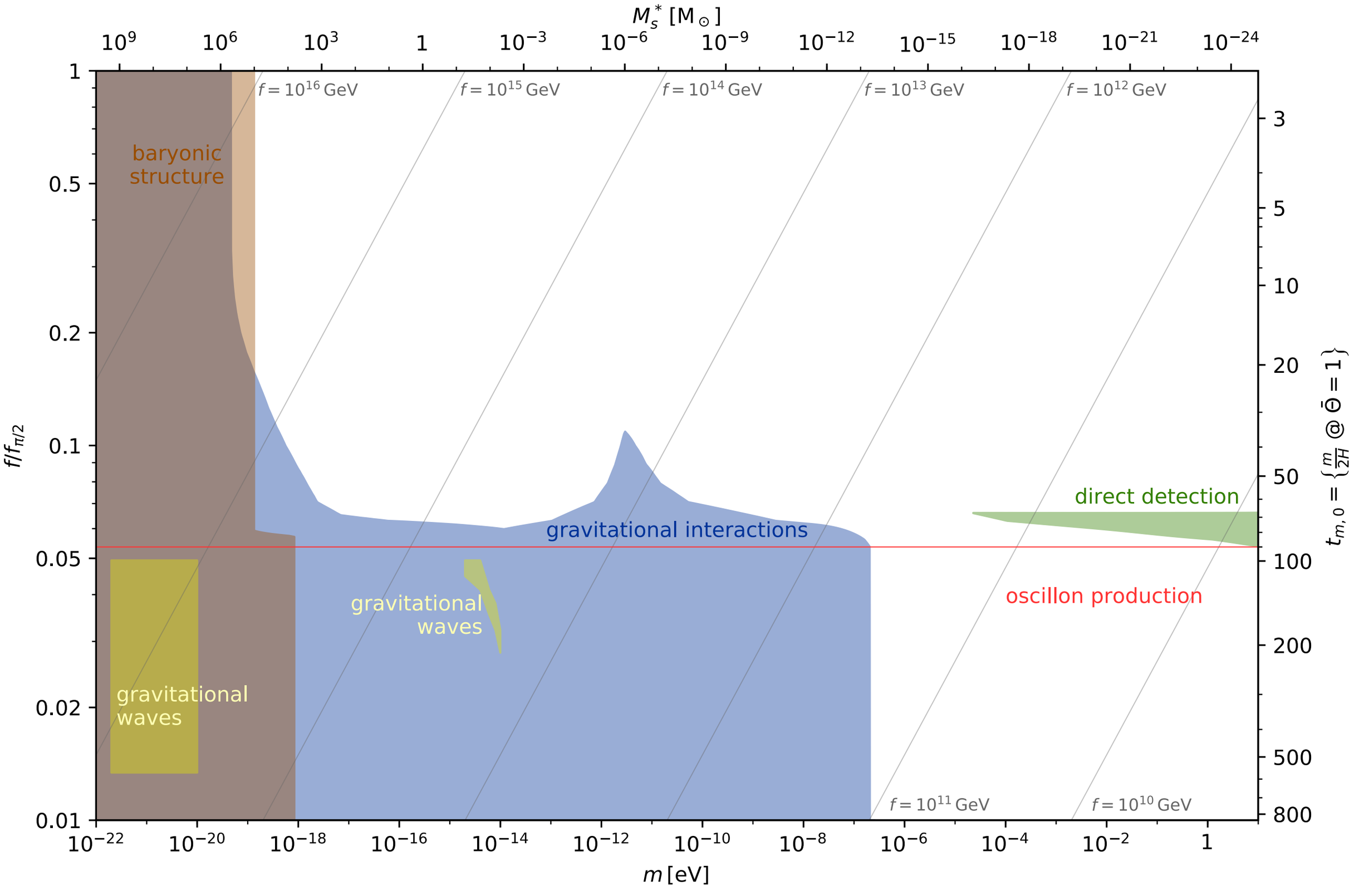
dense axion minihalos

solitons
[gravity+kinetic]

oscillons
[self-interactions+kinetic]



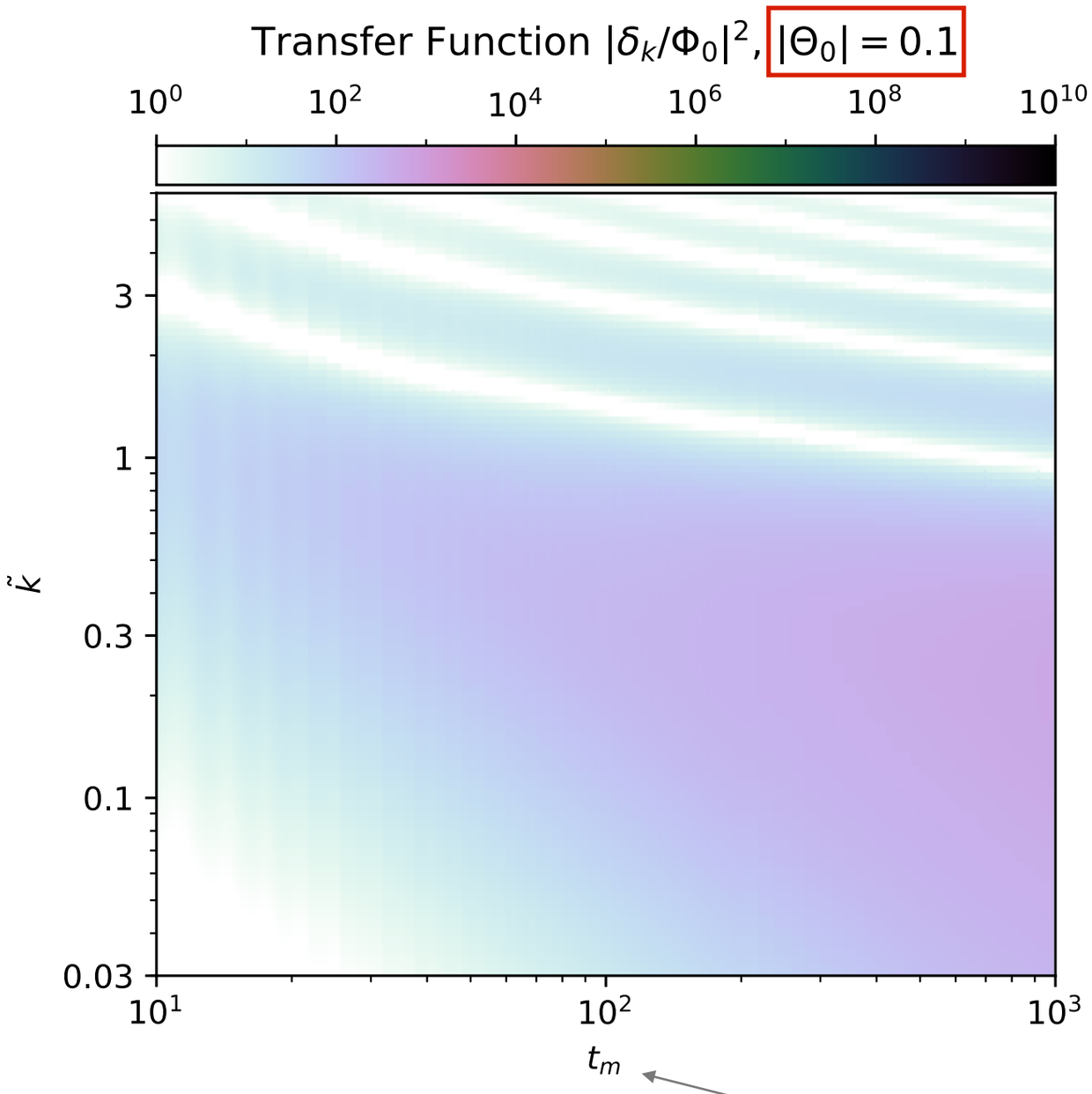
Observable Signatures

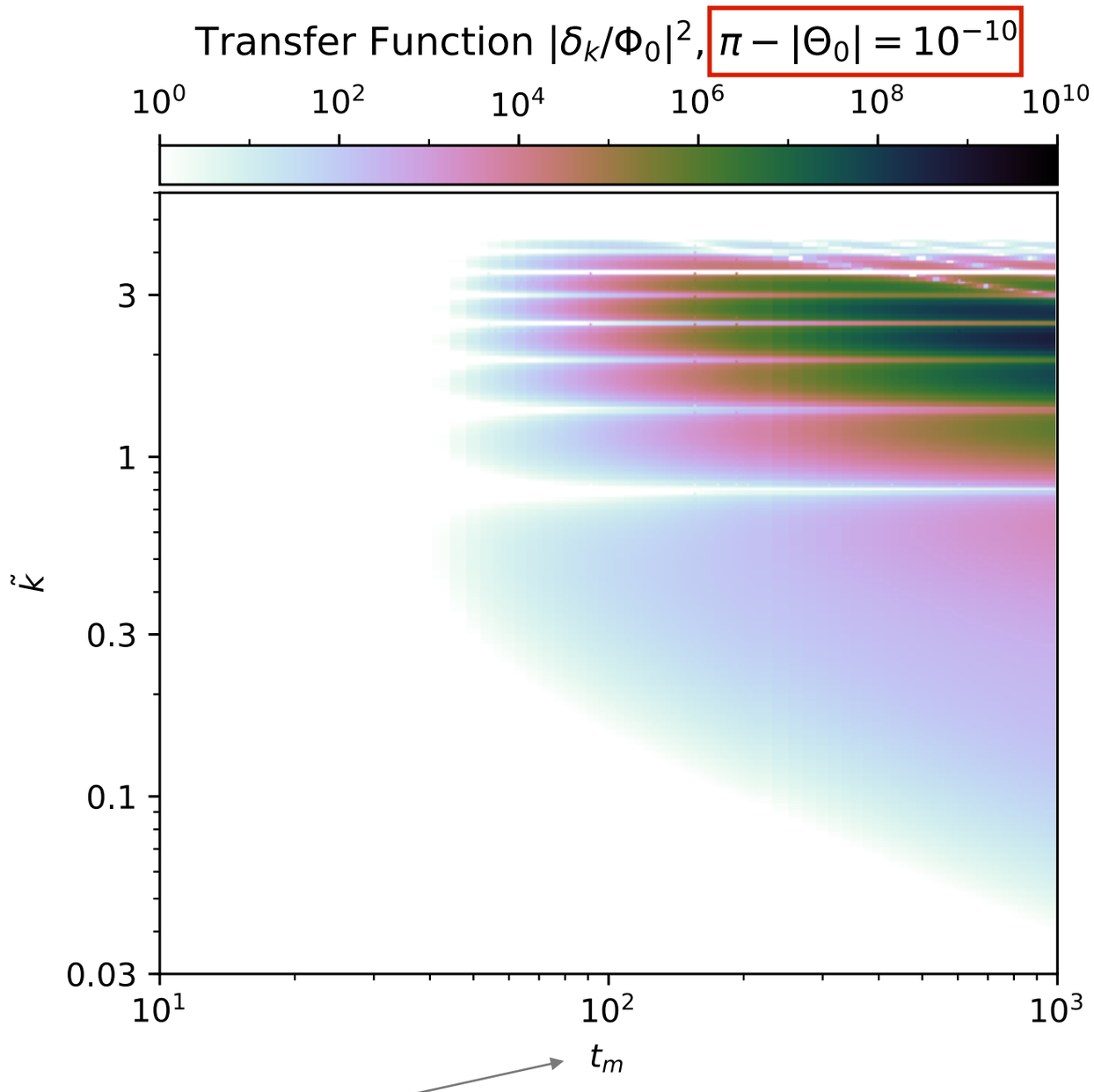


Linear Evolution in Time

small misalignment

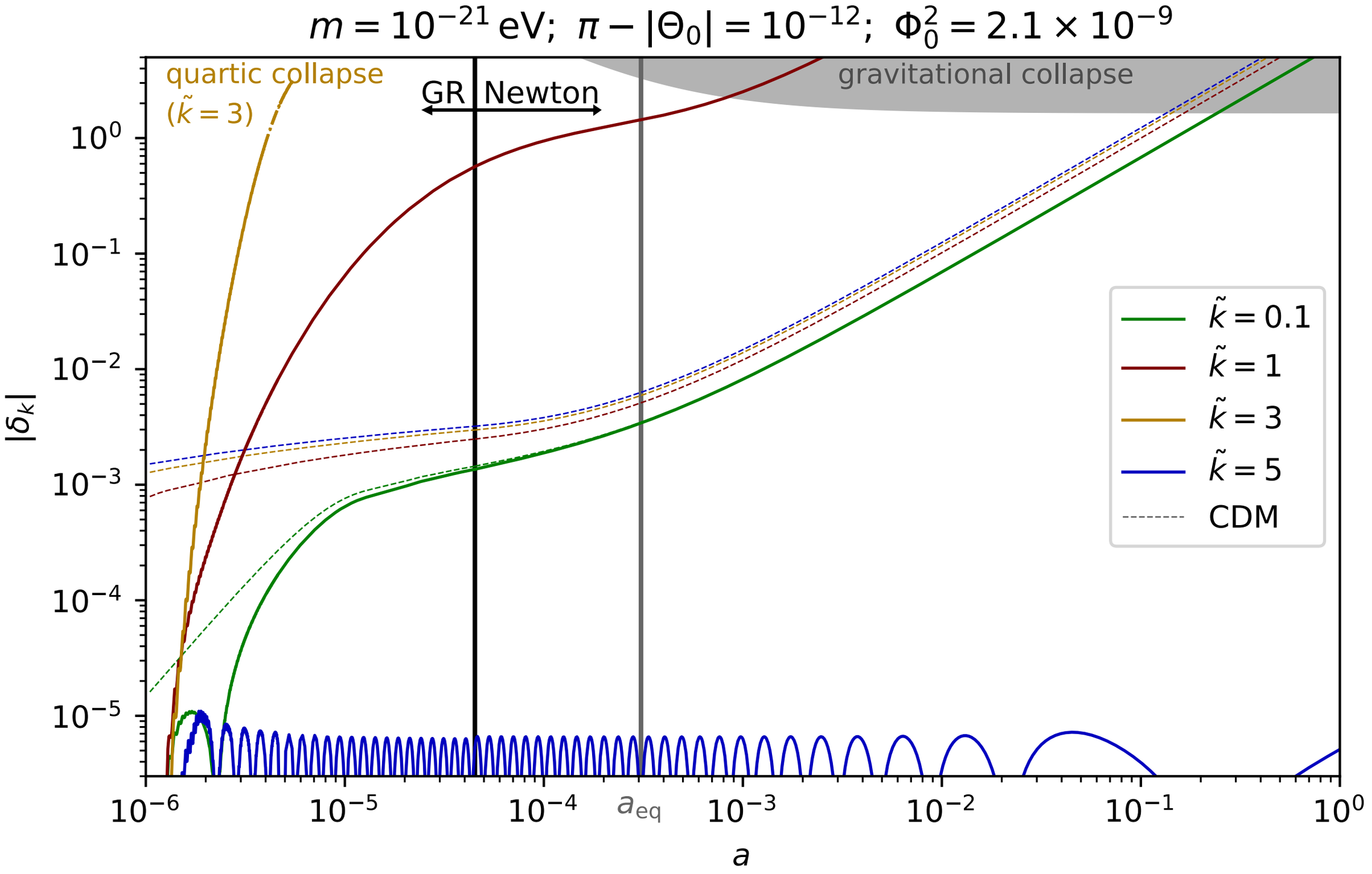
large misalignment



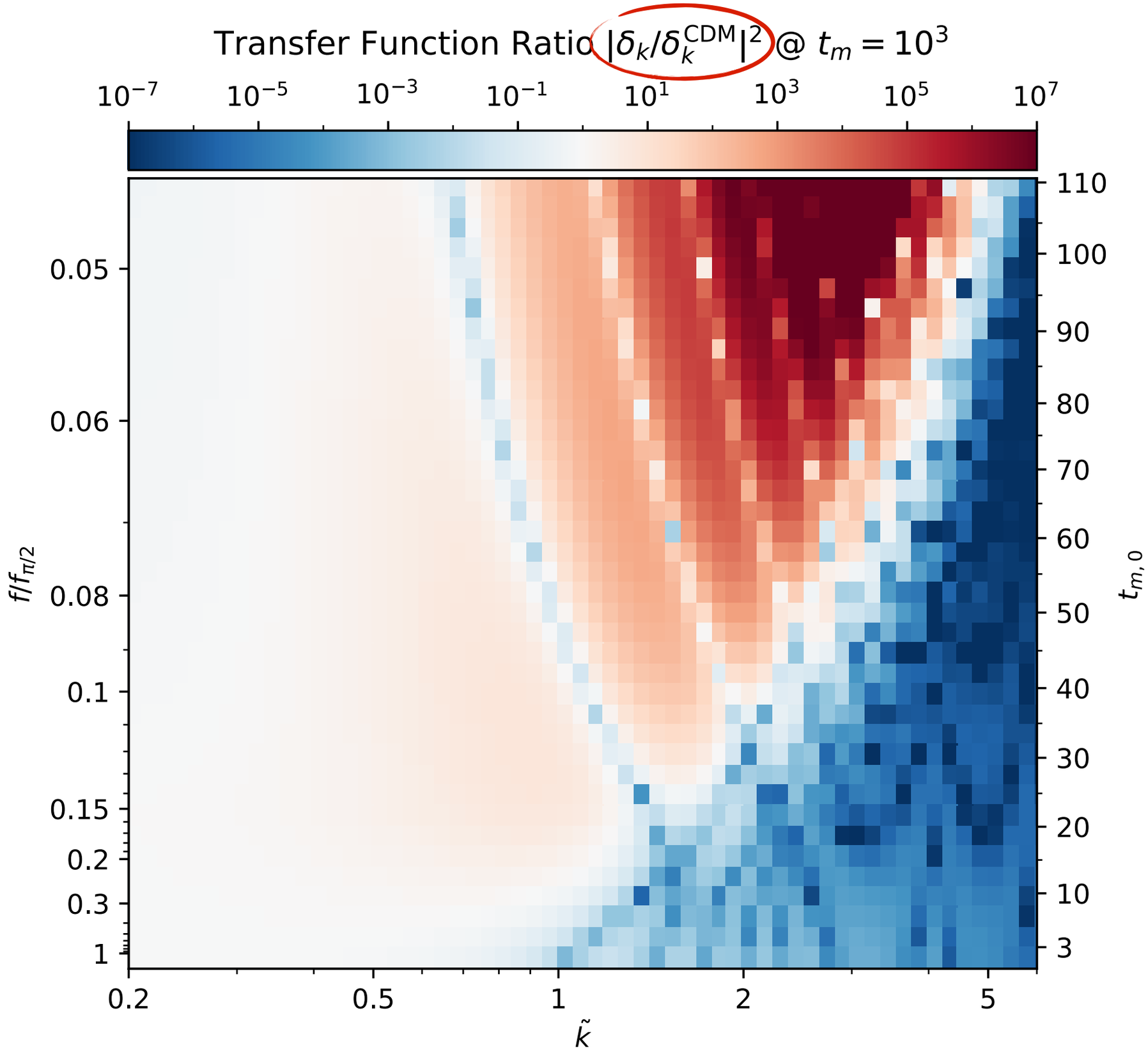


time in Compton units

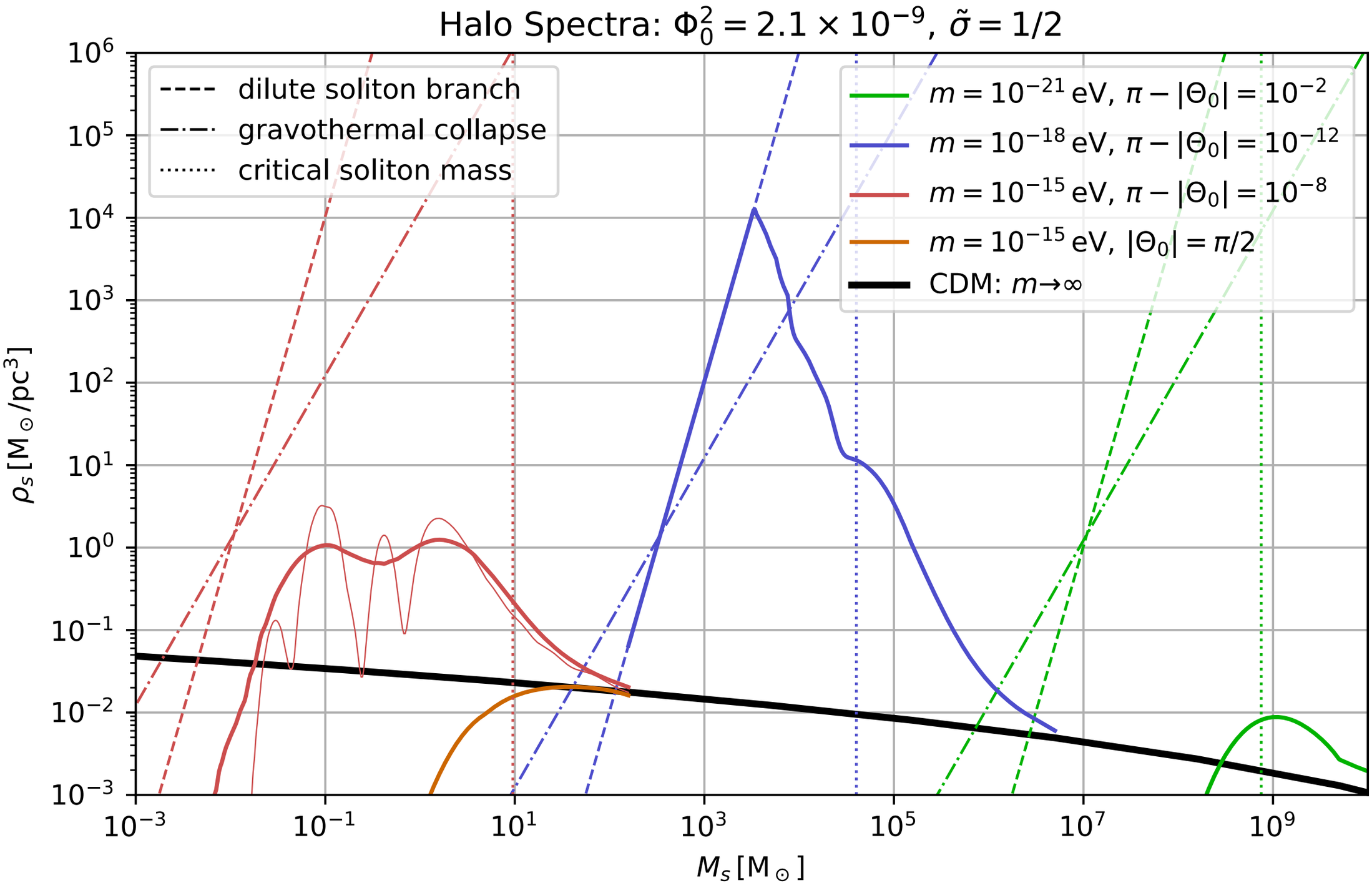
Linear Evolution in Time



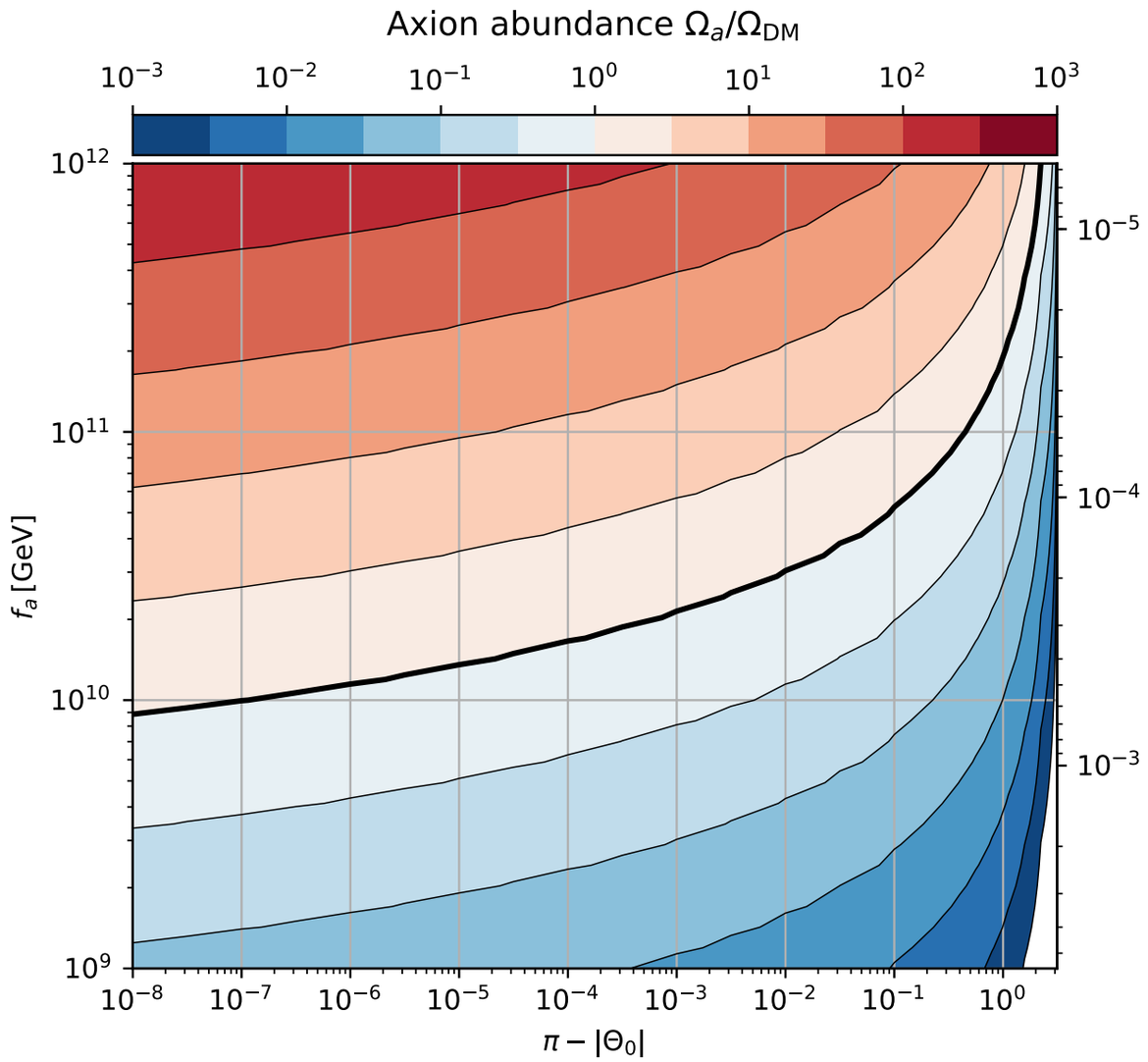
Linear Evolution versus Misalignment

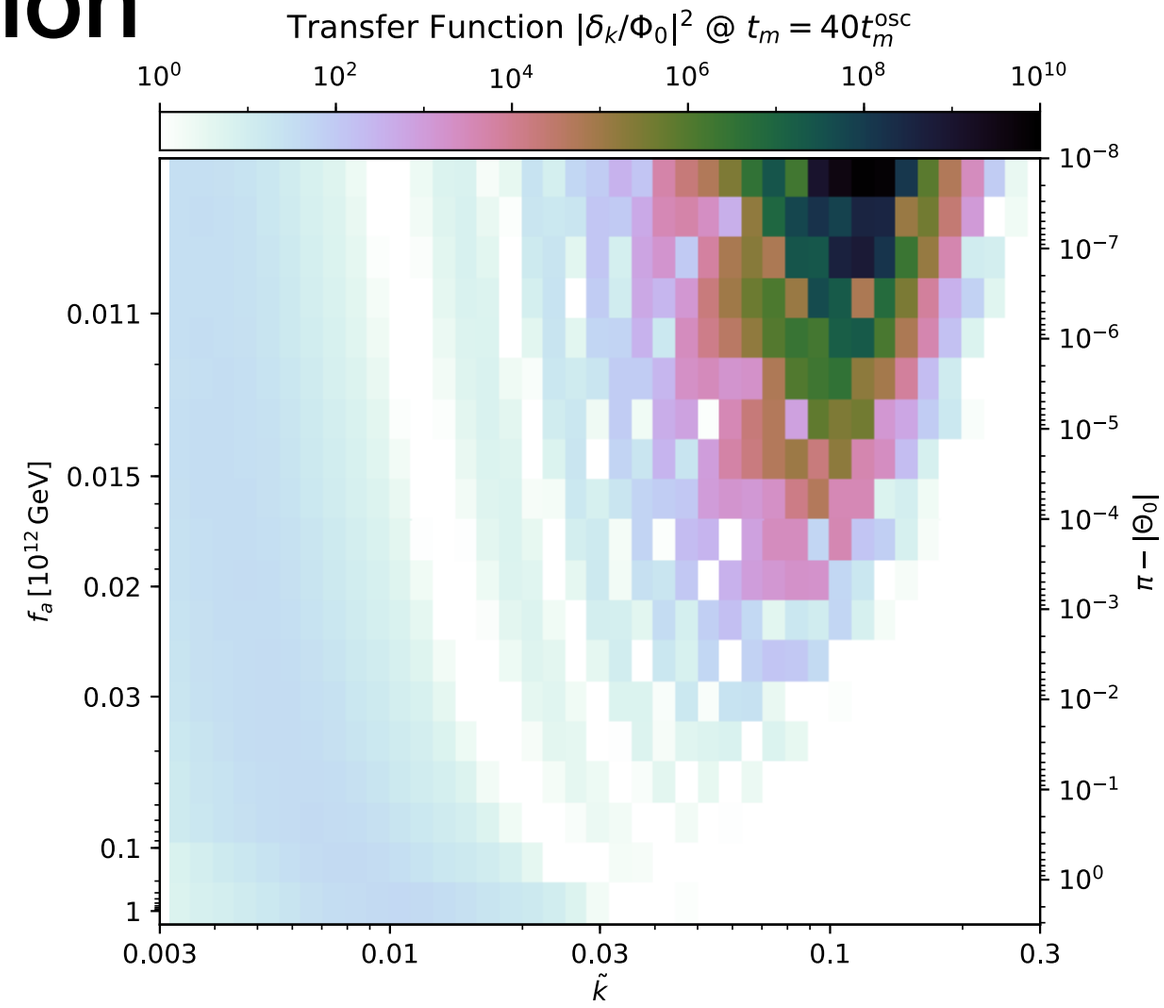


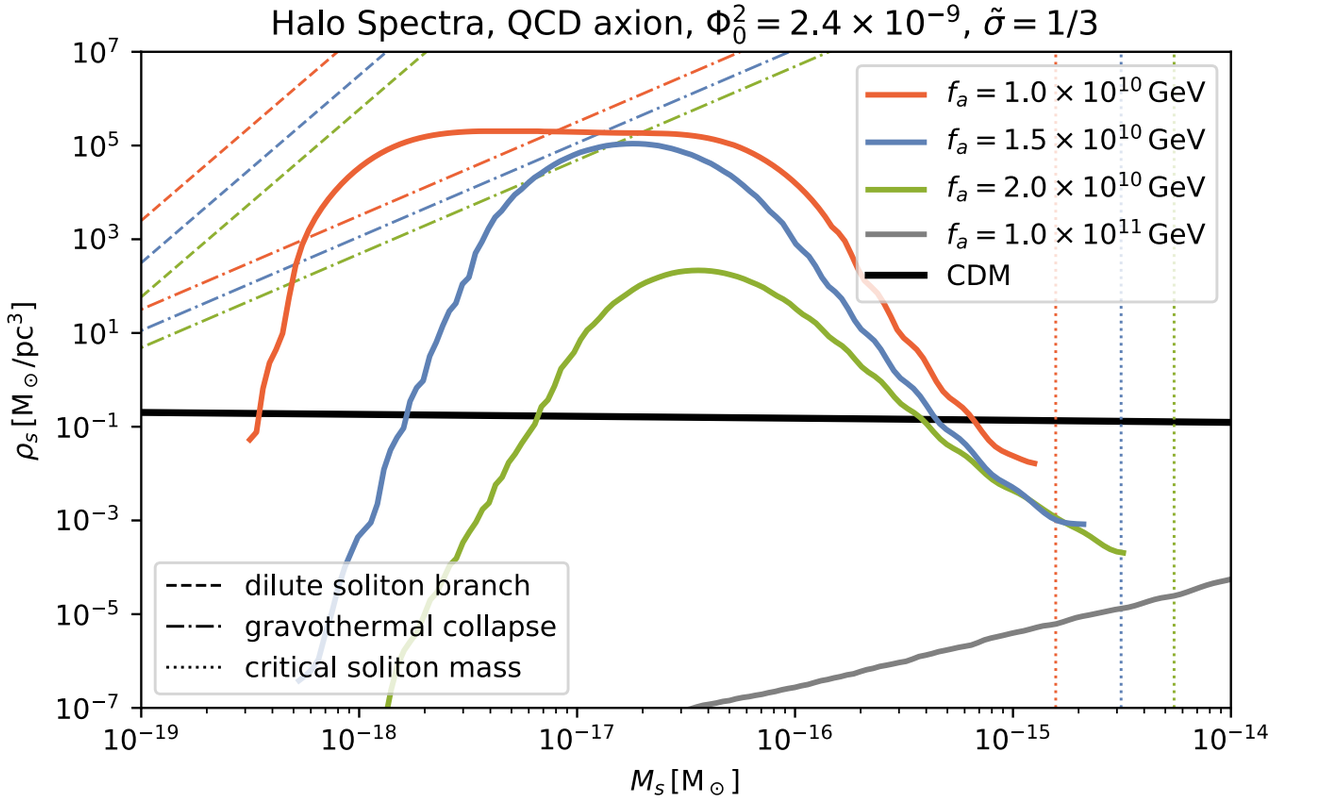
Dense Axion Halos & Solitons



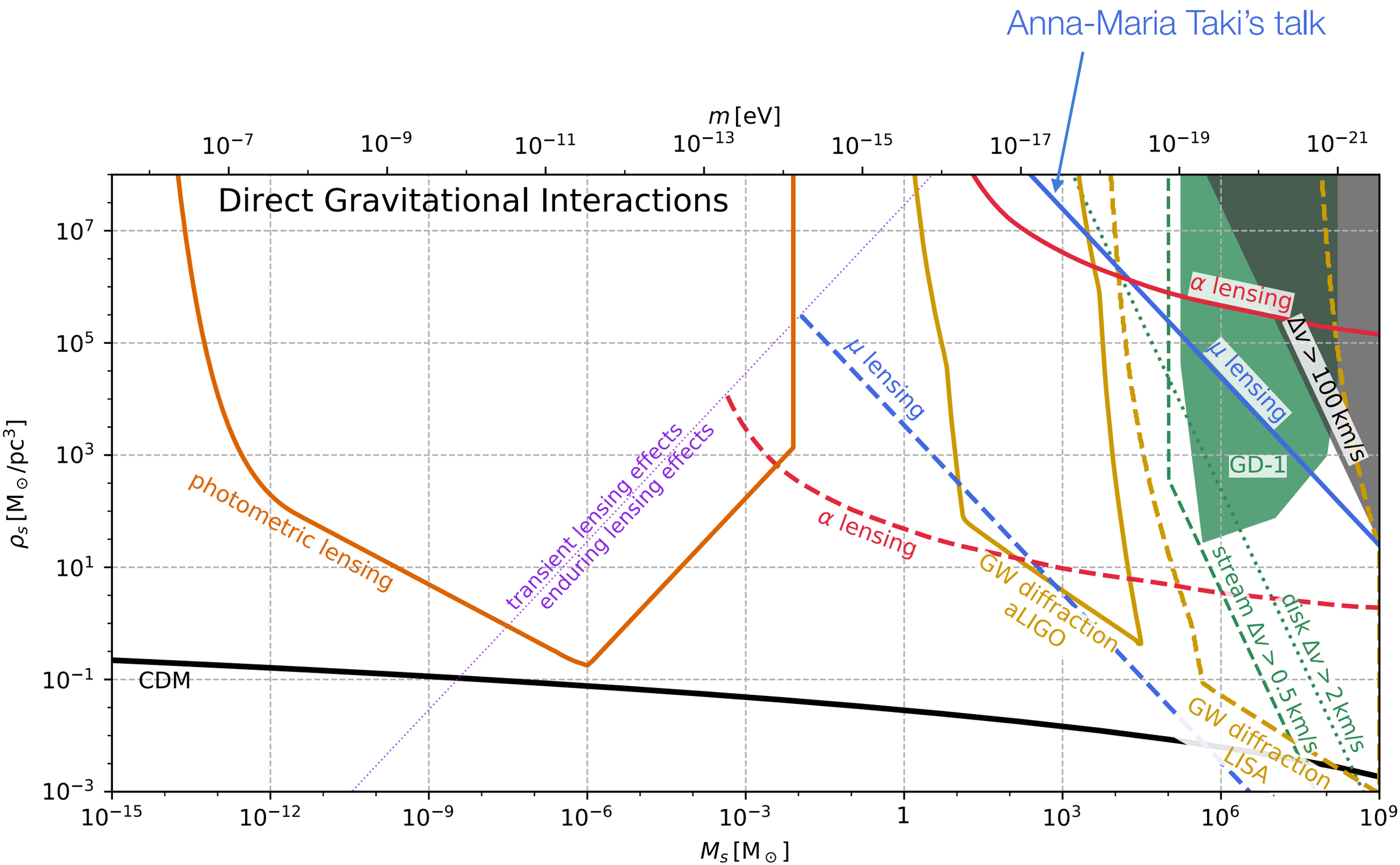
QCD Axion


Axion abundance $\Omega_a/\Omega_{\rm DM}$
10^{-3} 10^{-2} 10^{-1} 10^{0} 10^{1} 10^{2} 10^{3}
10^{12}
10^{11}
10^{10}
10^{9}
f_a [GeV]
10^{-5}
10^{-4}
10^{-3}
m_a [eV]
10^{-8} 10^{-7} 10^{-6} 10^{-5} 10^{-4} 10^{-3} 10^{-2} 10^{-1} 10^{0}
$\pi - |\Theta_0|$


Transfer Function $|\delta_k/\Phi_0|^2$ @ $t_m = 40 t_m^{\rm osc}$
10^{0} 10^{2} 10^{4} 10^{6} 10^{8} 10^{10}
0.011
0.015
0.02
0.03
0.1
1
$f_a\,[10^{12}\,{\rm GeV}]$
0.003 0.01 0.03 0.1 0.3
$\tilde{k}$
10^{-8} 10^{-7} 10^{-6} 10^{-5} 10^{-4} 10^{-3} 10^{-2} 10^{-1} 10^{0}
$\pi - |\Theta_0|$


Halo Spectra, QCD axion, $\Phi_0^2 = 2.4 \times 10^{-9}$, $\tilde{\sigma} = 1/3$
$f_a = 1.0 \times 10^{10}\,{\rm GeV}$
$f_a = 1.5 \times 10^{10}\,{\rm GeV}$
$f_a = 2.0 \times 10^{10}\,{\rm GeV}$
$f_a = 1.0 \times 10^{11}\,{\rm GeV}$
CDM
dilute soliton branch
gravothermal collapse
critical soliton mass
$\rho_s\,[{\rm M}_\odot/{\rm pc}^3]$
10^{7} 10^{5} 10^{3} 10^{1} 10^{-1} 10^{-3} 10^{-5} 10^{-7}
10^{-19} 10^{-18} 10^{-17} 10^{-16} 10^{-15} 10^{-14}
$M_s\,[{\rm M}_\odot]$

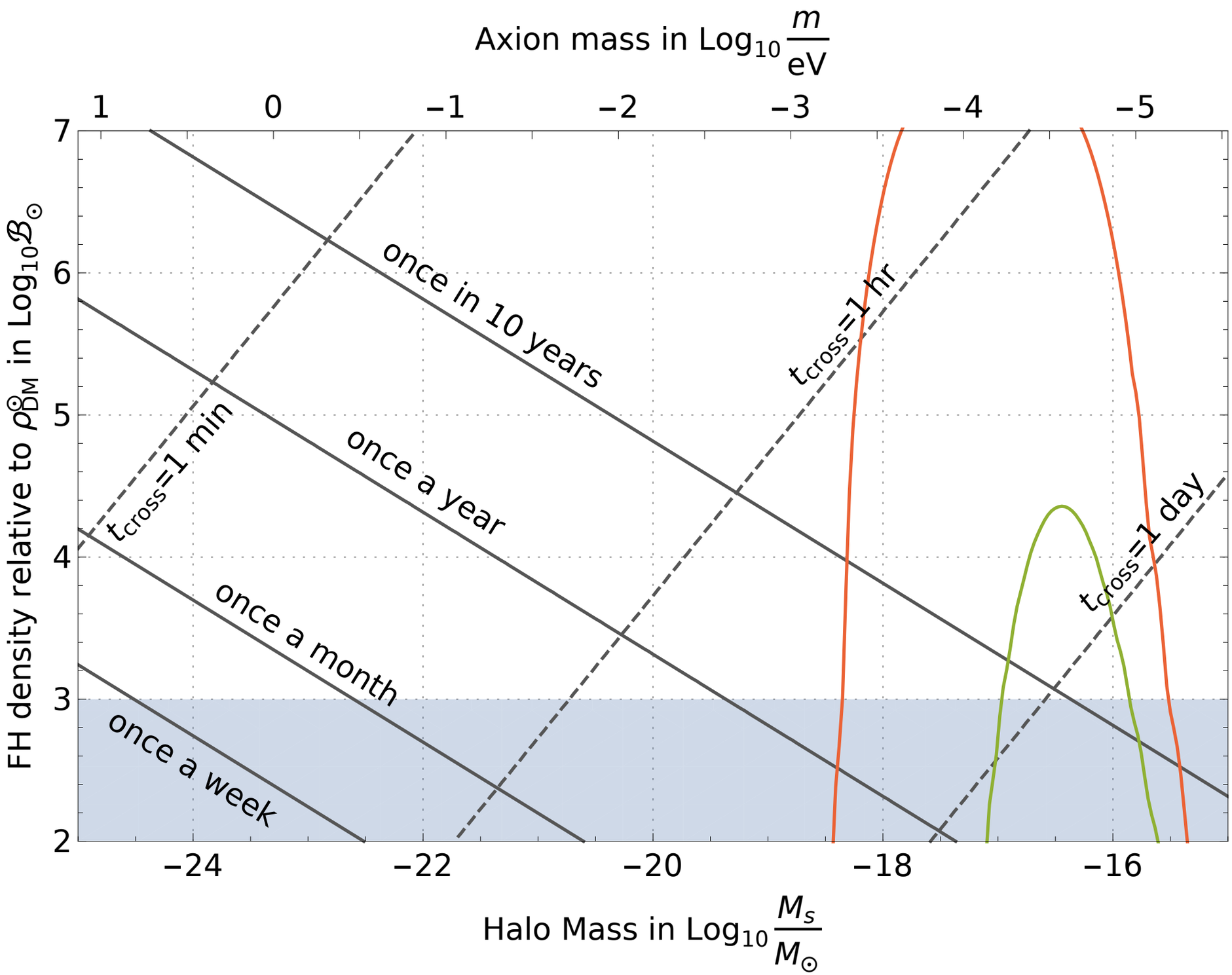
Gravitational Interactions



Direct Detection

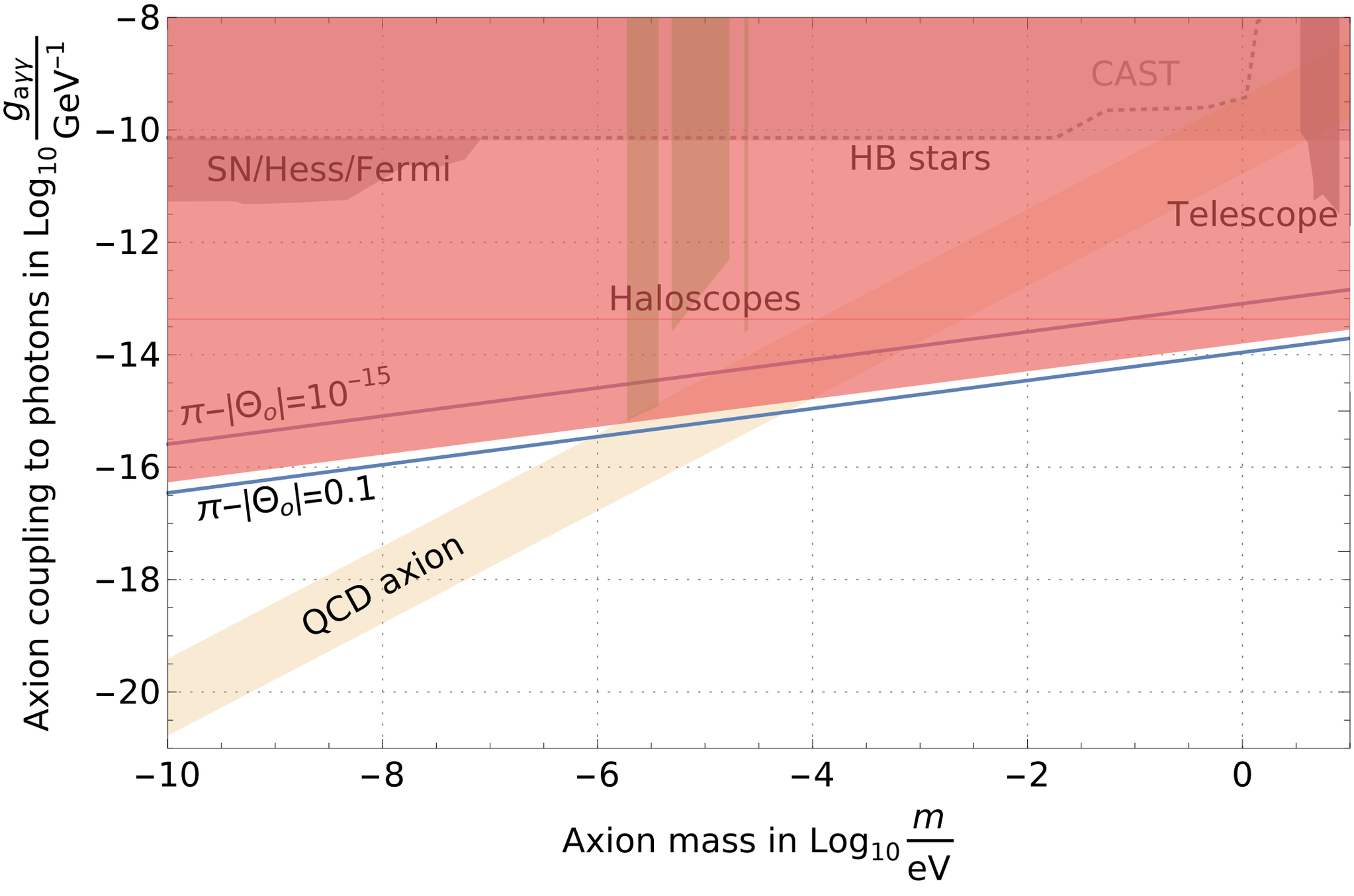
intermittent, highly coherent signals ⟶ broadband data recording

matched filters



Direct Detection

re-evaluate constraints and optimize high-frequency axion searches

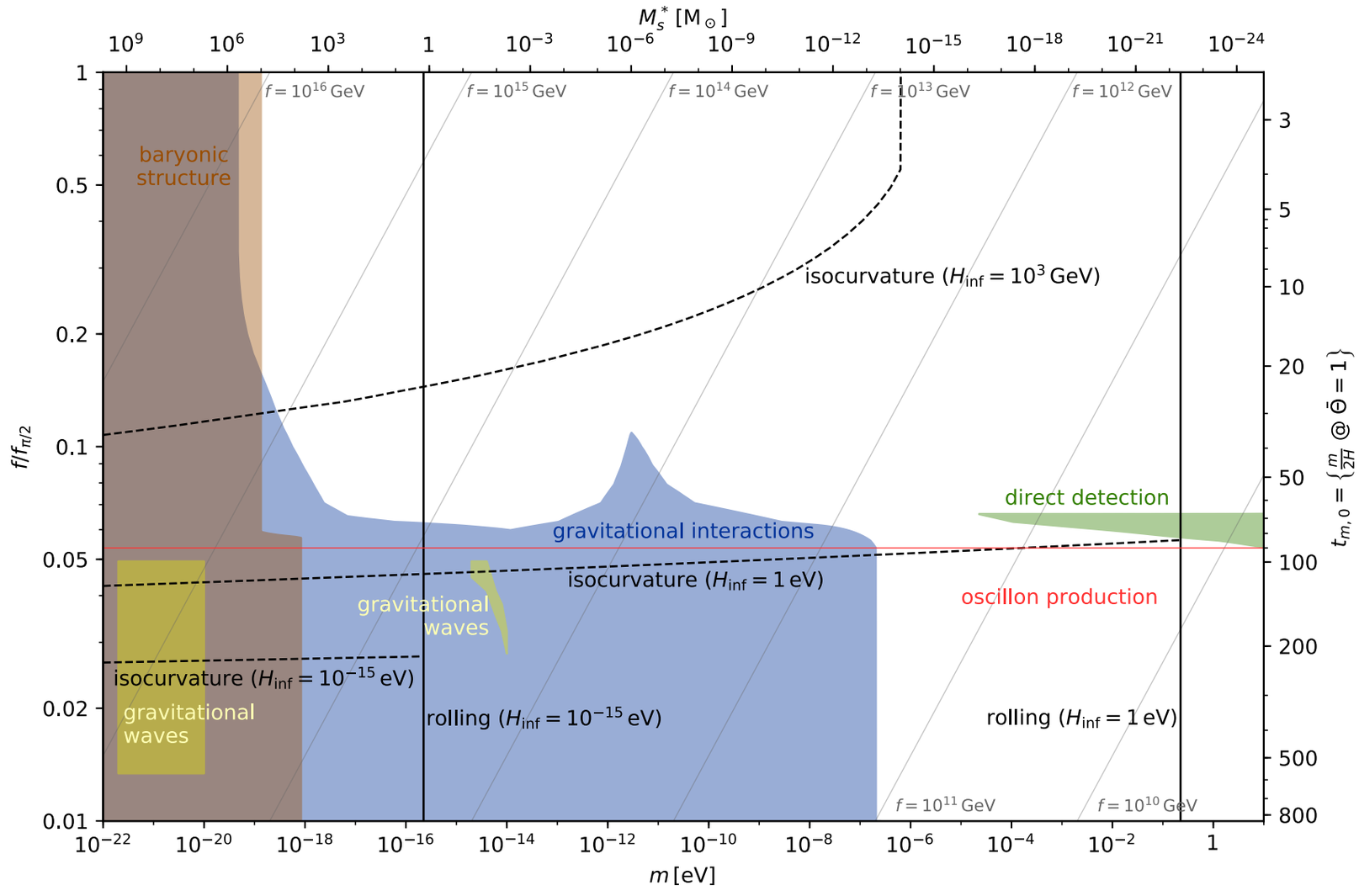


Summary

If the onset of axion oscillations is delayed such that

nonlinearities > Hubble friction, i.e. $\bar{\Theta}^2 \gtrsim \frac{4m}{H}$,

then semi-relativistic fluctuations grow exponentially to form compact axion structures

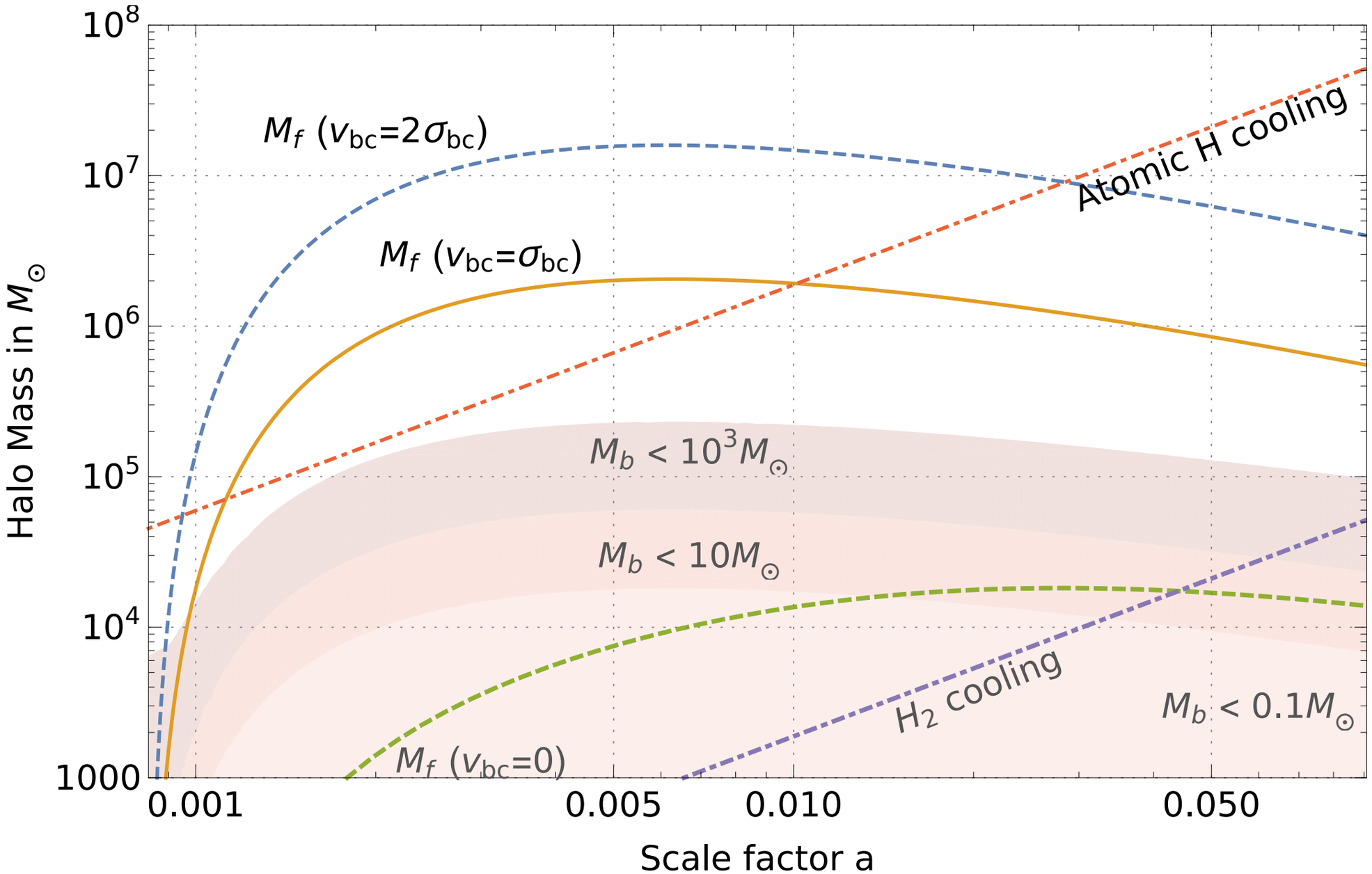


Open Questions:

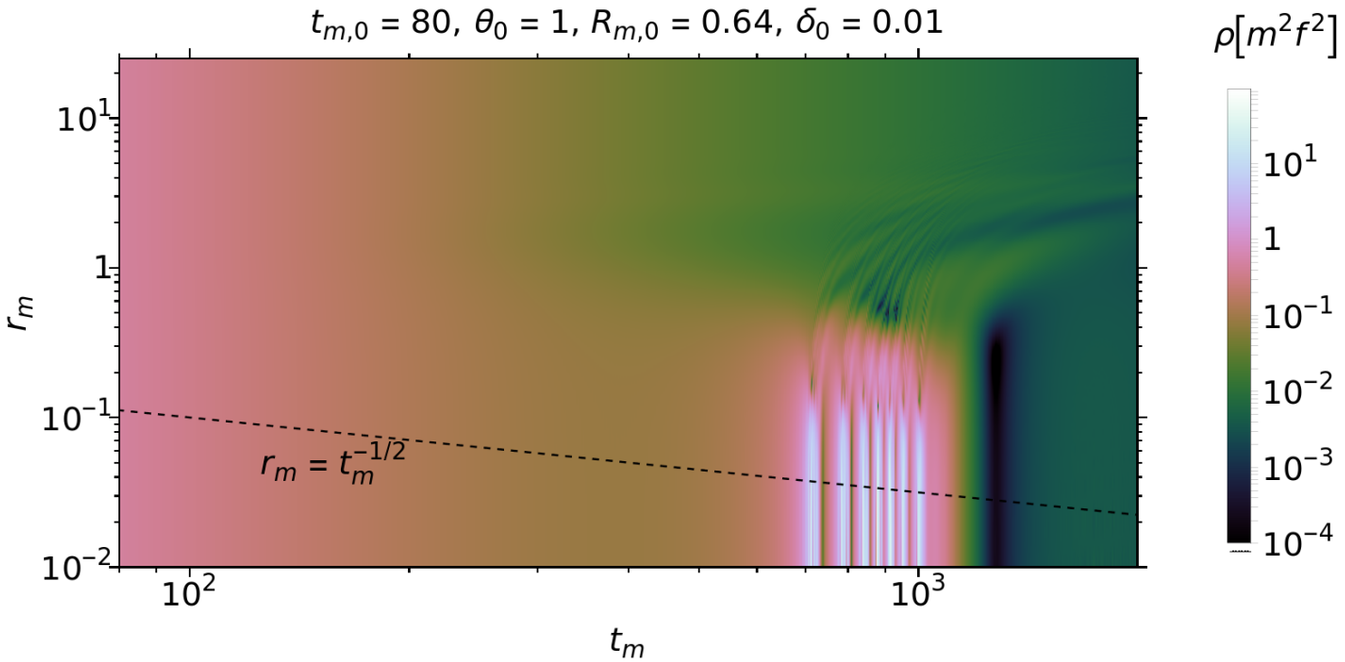
1. Nonlinear simulations:
   — tidal stripping
   — gravitational cooling
   — oscillon dynamics
   — GW production
2. Impact on direct detection
3. Star formation & re-ionization history
4. Analytic estimates of oscillon lifetime

Backup

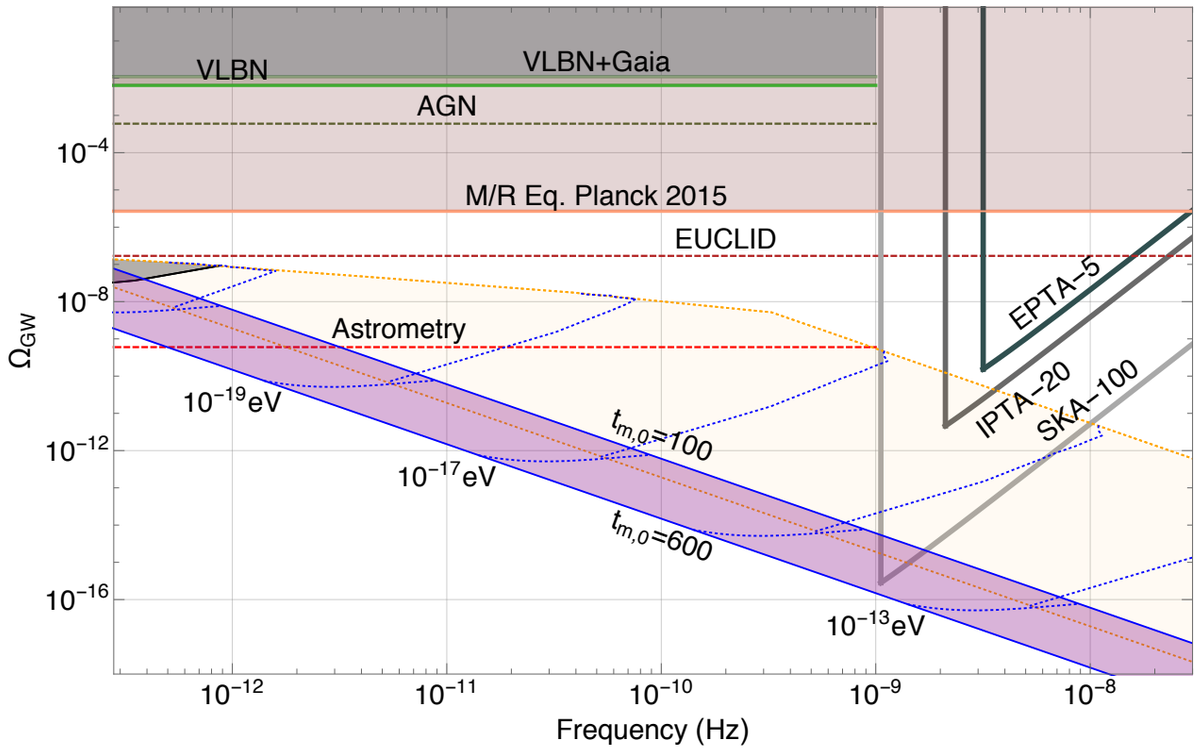
Baryonic Structure & Star Formation

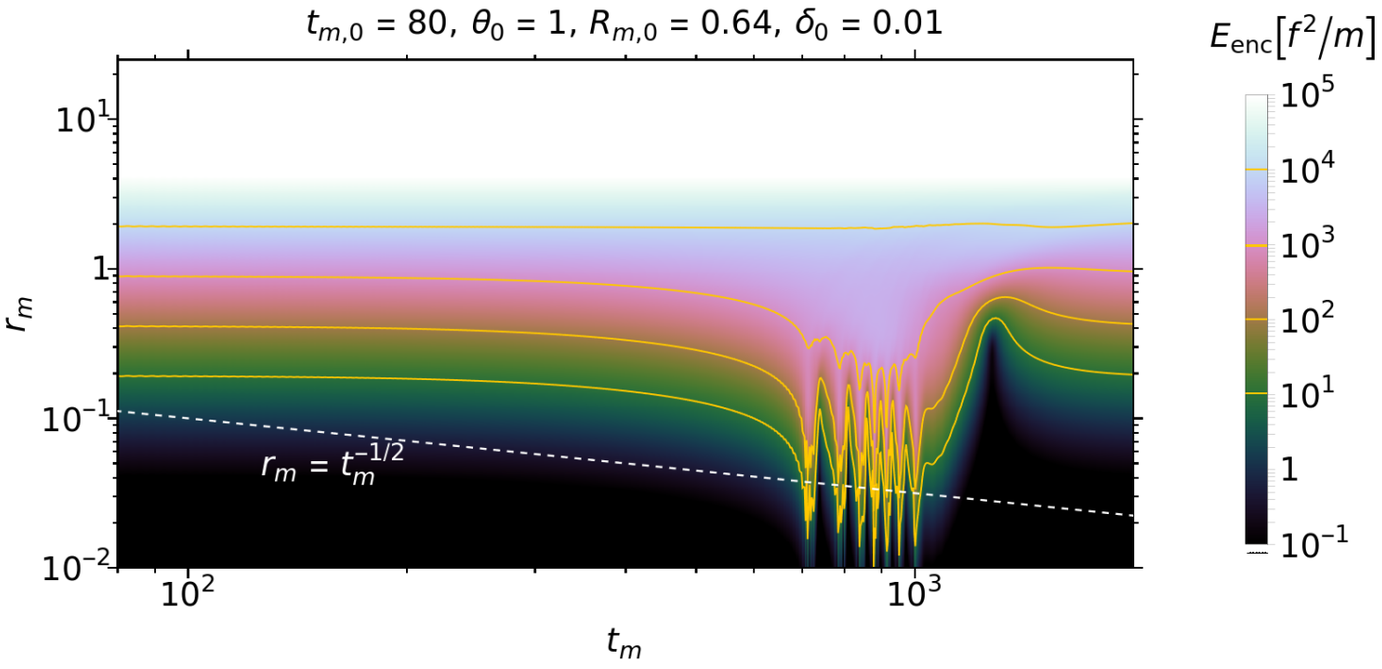


Oscillon Production



Gravitational Waves

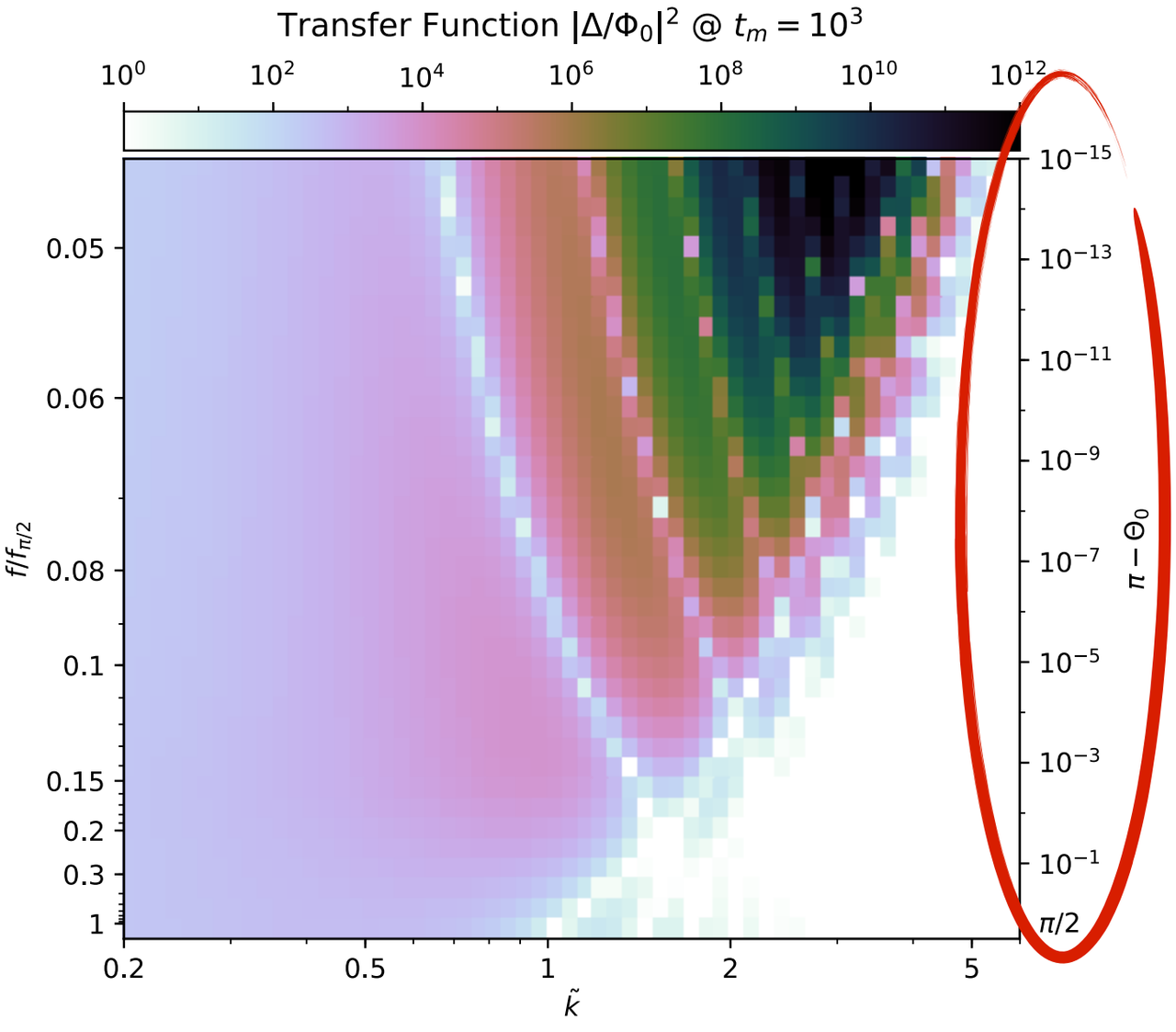




Initial Conditions

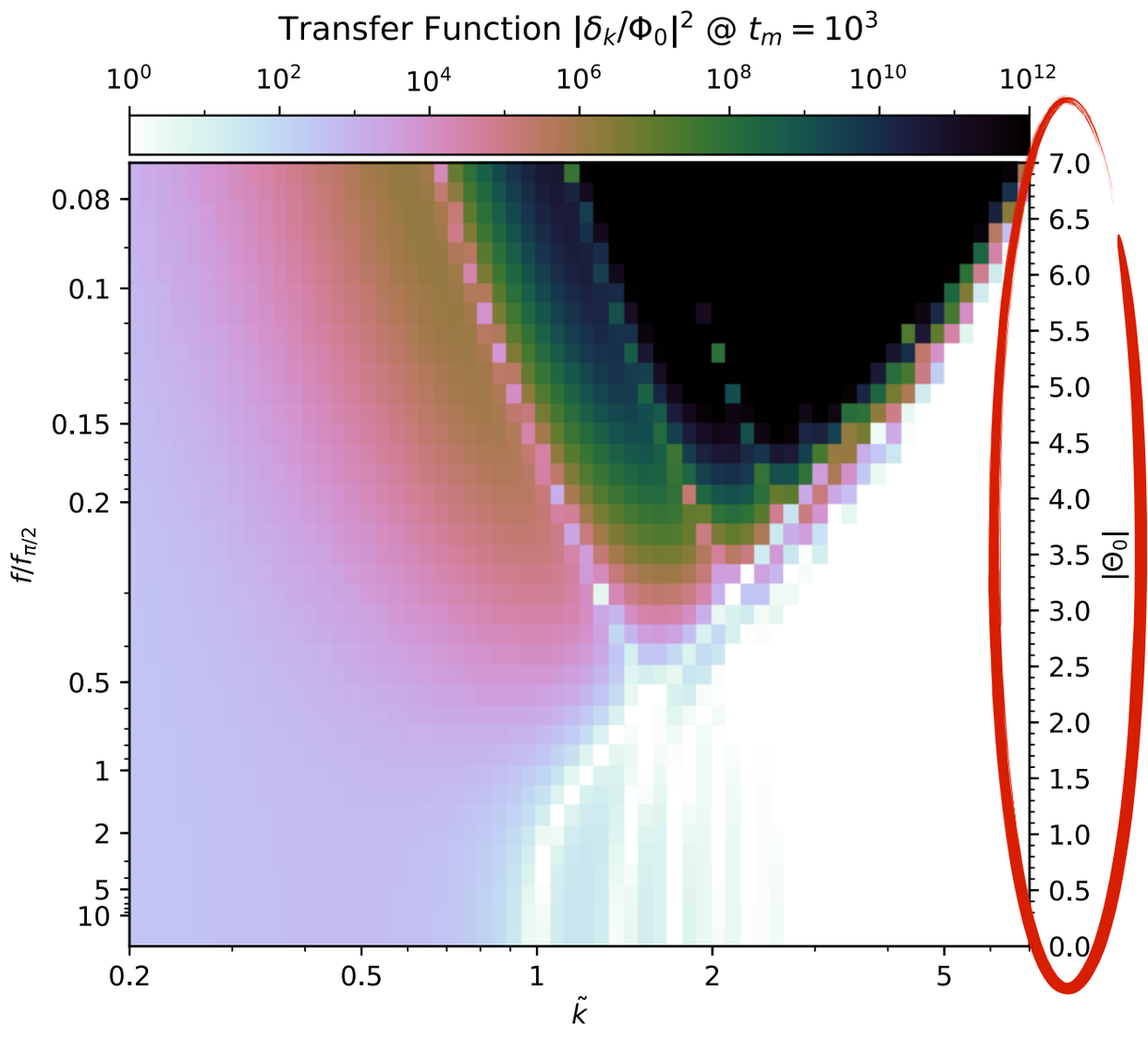
1. inflationary dynamics for $|\Theta_0| \simeq \pi$

2. environmental selection on DM abundance



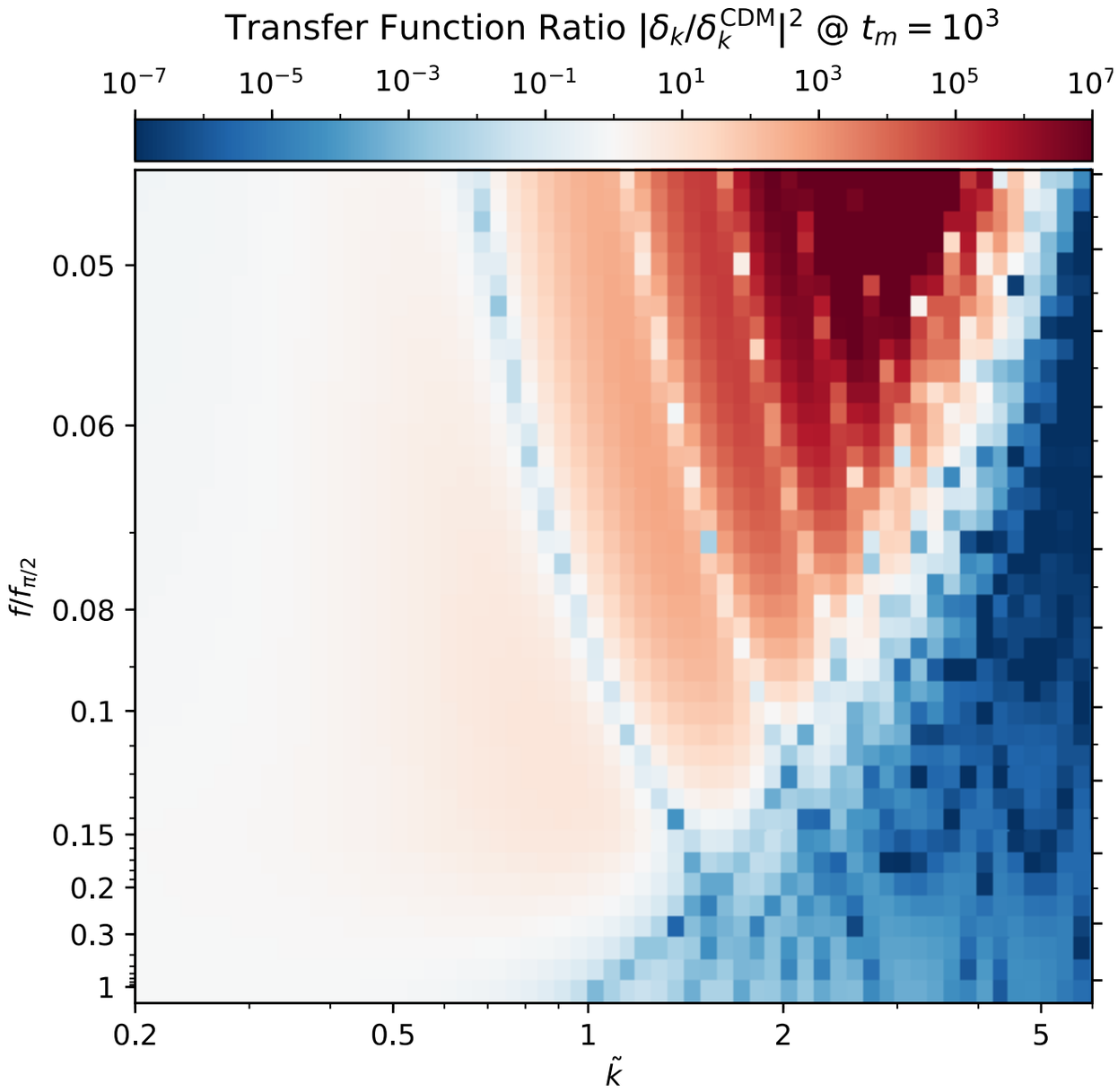
$$V(\Theta) \propto (1 - \cos(\Theta))$$

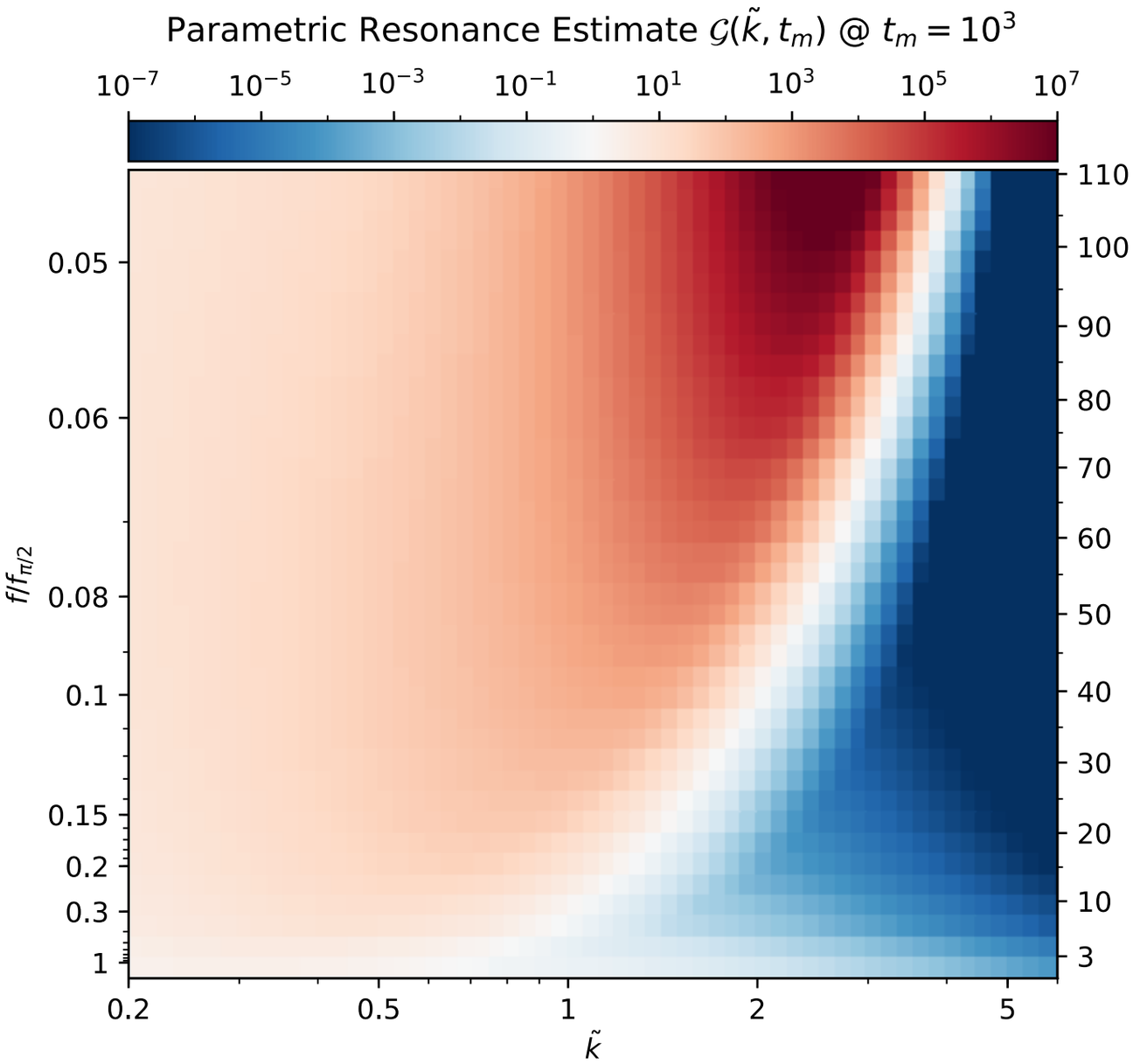
3. large misalignment in other potentials:



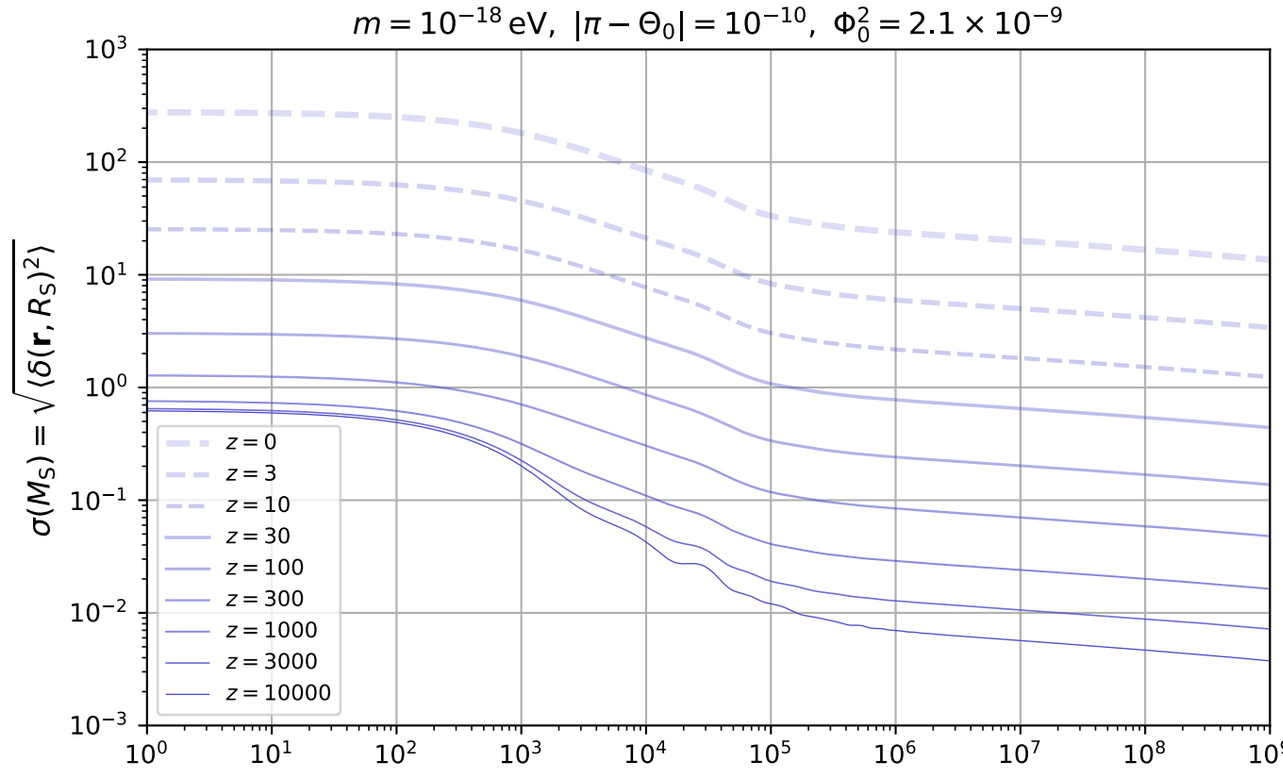
$$V(\Theta) \propto \frac{\Theta^2}{2 + \Theta^2}$$

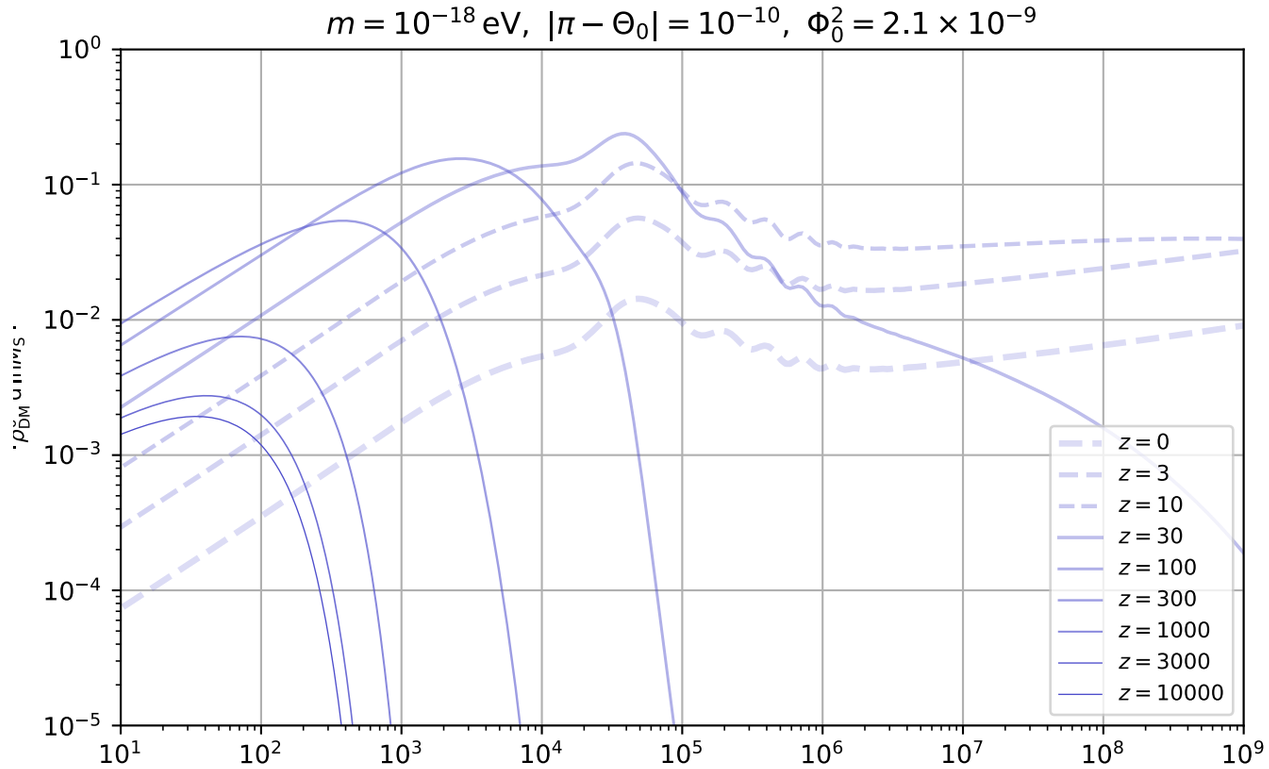
Parametric resonance

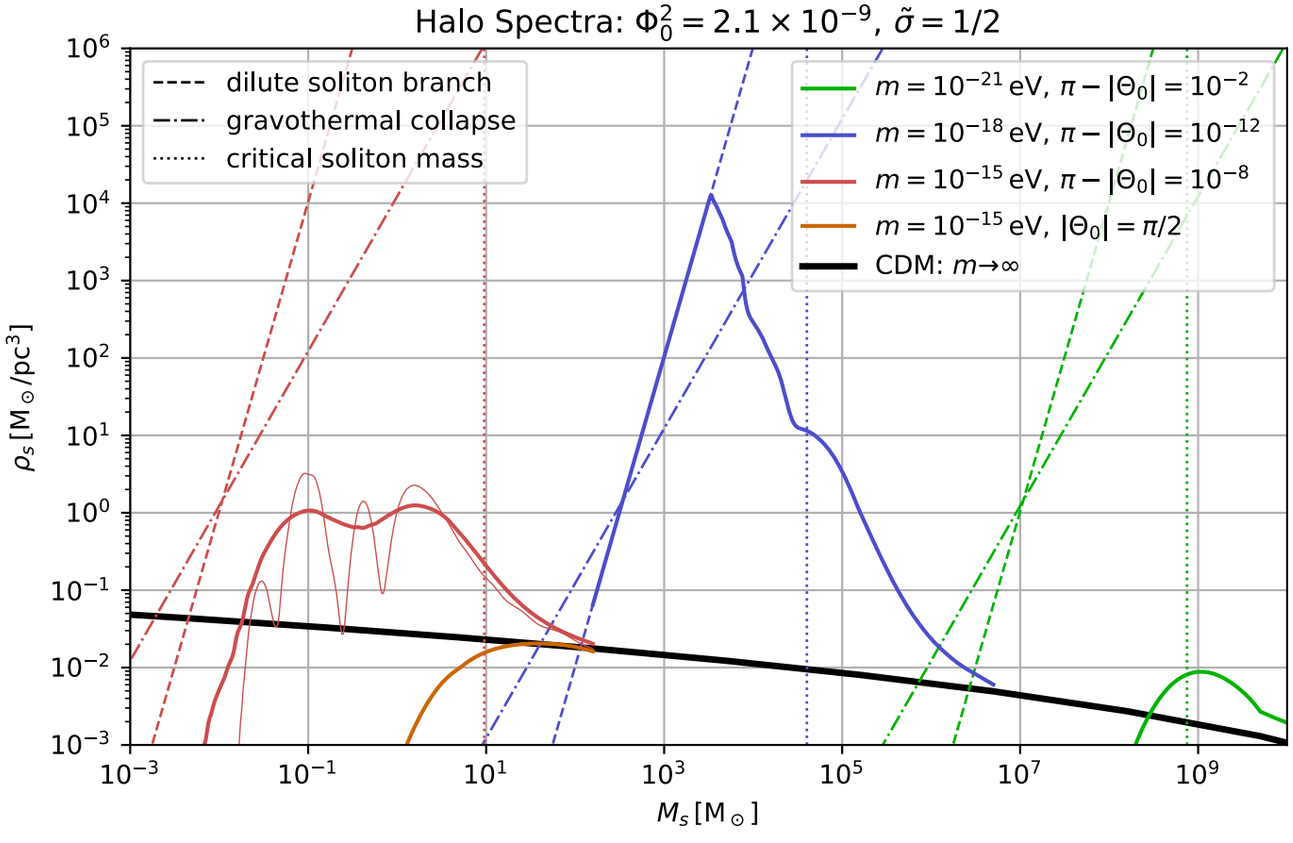




Press-Schechter







Condition for Oscillon Formation